

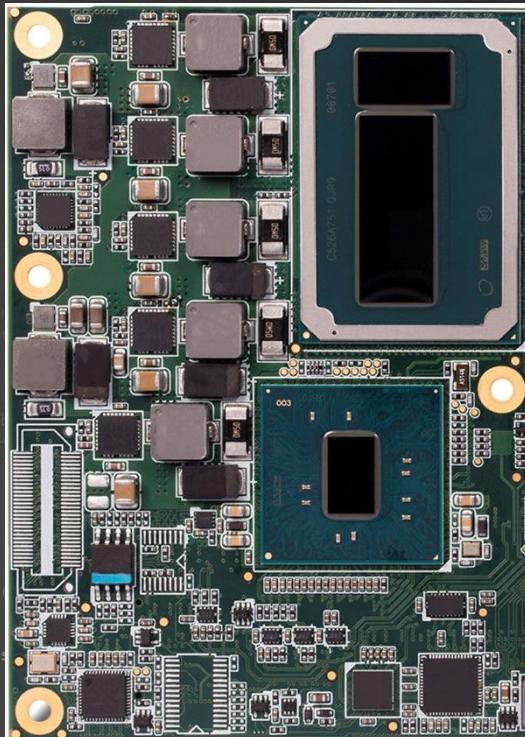
/INFOMOV/ Optimization & Vectorization

J. Bikker - April - June 2024 - Lecture 5: "SIMD (1)"

Welcome!



Meanwhile, on



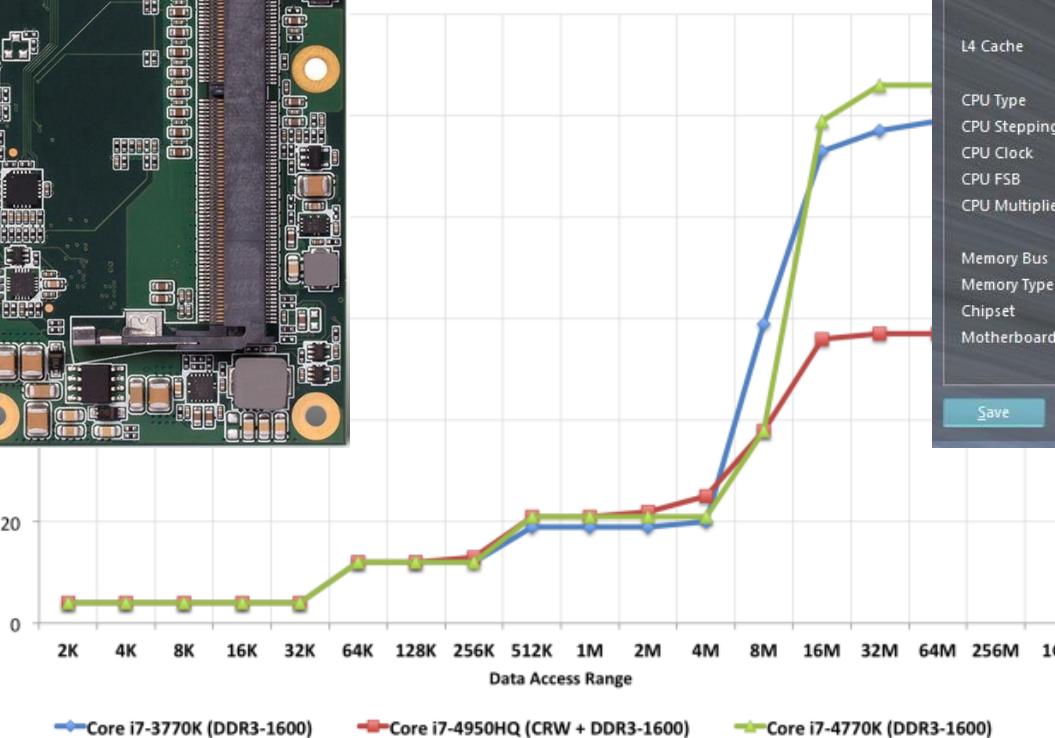
Crystalwell Architecture

Unlike previous eDRAM implementations in game consoles, Crystalwell is true 4th level cache in the memory hierarchy. It acts as a victim buffer to the L3 cache, meaning anything evicted from L3 cache immediately goes into the L4 cache. Both CPU and GPU requests are cached. The cache can dynamically allocate its partitioning between CPU and GPU use. If you don't use the GPU at all (e.g. discrete GPU installed)

PU requests. That's right, Haswell CPUs equipped with

connection to Crystalwell other than to say that it's a native 50GB/s bi-directional bandwidth (100GB/s aggregate) 30 - 32ns, nicely in between an L3 and main memory access

Latency vs. Access Range (Sandra 2013 SP3)



	Read	Write	Copy	Latency
Memory	29595 MB/s	28986 MB/s	33343 MB/s	62.9 ns
L1 Cache	878.58 GB/s	448.80 GB/s	892.60 GB/s	1.1 ns
L2 Cache	352.03 GB/s	143.62 GB/s	215.68 GB/s	3.3 ns
L3 Cache	176.35 GB/s	114.56 GB/s	128.93 GB/s	12.8 ns
L4 Cache	48206 MB/s	33682 MB/s	42269 MB/s	42.4 ns
CPU Type	QuadCore Intel Core i7-5775C (Broadwell-H, LGA1150)			
CPU Stepping	E0/G0			
CPU Clock	3699.8 MHz (original: 3300 MHz, overclock: 12%)			
CPU FSB	100.0 MHz (original: 100 MHz)			
CPU Multiplier	37x			
North Bridge Clock	3299.8 MHz			
Memory Bus	933.3 MHz	DRAM:FSB Ratio	28:3	
Memory Type	Dual Channel DDR3-1866 SDRAM (11-13-13-35 CR1)			
Chipset	Intel Wildcat Point Z97, Intel Broadwell-H			
Motherboard	Asus Maximus VII Ranger			
AIDA64 v5.20.3440 Beta / BenchDLL 4.1.633-x64 (c) 1995-2015 FinalWire Ltd.				

The eDRAM clock tops out at 1.6GHz.

There's only a single size of eDRAM offered this generation: 128MB. Since it's a cache and not a buffer (and a giant one at that), Intel found that hit rate rarely dropped below 95%. It turns out that for current workloads, Intel didn't see much benefit beyond a 32MB eDRAM however it wanted the design to be future proof. Intel

Meanwhile, the job market

```

    & (depth < MAXDEPTH)

    c = inside ? 1 : 1.0f;
    nt = nt / nc, ddn = ddn / nc;
    os2t = 1.0f - nnt * nnt;
    o, N );
    b);

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - RE)
    at) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;

    -
    refl + refr)) && (depth < MAXDEPTH)

    o, N );
    refl * E * diffuse;
    = true;

MAXDEPTH)

    psurvive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &lightDir,
    e.x + radiance.y + radiance.z) > 0) && (dot( N, L ) > 0);

    v = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Schlick's
    /alive)

    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
    urvive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

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- **OpenCL/CUDA expert** (Also accepting freelancers)
- **Sales support**

The procedure for the technical roles is as follows:

- You send a CV and tell us why you are the perfect candidate.
- After that you are invited for a longer online test. You show your skills on C/C++ and algorithms. You will receive a PDF with useful feedback.
- If you selected GPGPU or mentioned it, we send you a GPU assignment. You need to pick out the right optimisations, code it and explain your decisions. (Hopefully under 30 minutes)
- If all goes well, you'll have a videochat with Vincent (CEO) on personal and practical matters. You can also ask us anything, to find out if we fit you. (Around 1 hour)

Meanwhile, P2

```

rics
k (depth < MAXDEPTH)
    c = inside ? 1 : 1.2f;
    nt = nt / nc, ddn = ddn / nc;
    pos2t = 1.0f - nnt * nnt;
    D, N );
}
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;
    if (refl + refr) && (depth < MAXDEPTH)
        D, N );
        refl * E * diffuse;
        = true;
MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closer);
if;
radiance = SampleLight( &rand, I, &L, &light);
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e = true;
at brdfPpdf = EvaluateDiffuse( L, N ) * Psurvive;
at t3 factor = diffuse * INVPI;
at weight = Mis2( directPpdf, brdfPpdf );
at cosThetaOut = dot( N, L );
E * (weight * cosThetaOut) / directPpdf) * (radiance
random walk - done properly, closely following Smiley
alive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;

```

Assignment P2 – Cache Simulator

Formal assignment description for P2 - INFOMOV
Jacco Bikker, 2024



Universiteit Utrecht

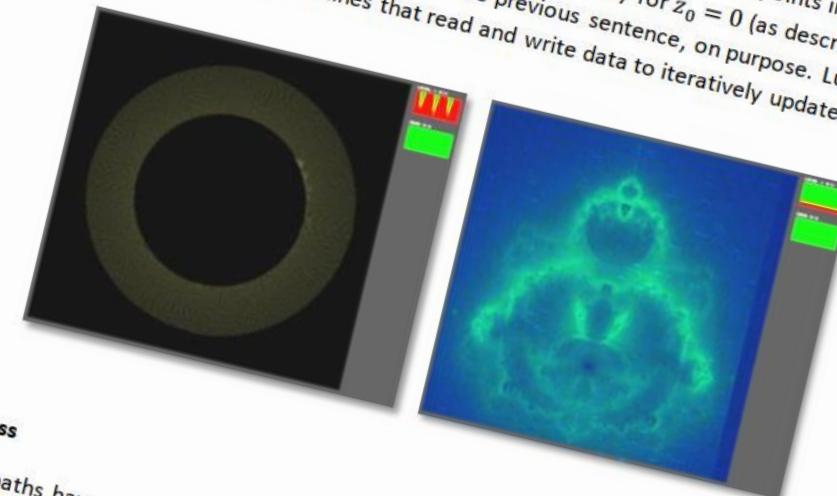
Introduction

This document describes the requirements for the second assignment for the INFOMOV course. For this assignment, you will extend a simple cache simulator, which currently implements a fully associative cache.

Base Code

The base code in game.cpp renders a spiral. The contents of a simulated two-level memory system (L1 cache + RAM) are visualized in real-time: bright colors are cached; darker ones reside in ‘DRAM’. The provided fully associative cache uses a random eviction policy, so pixels of the spiral will randomly leave the cache, resulting in a pretty sparkly trail.

An alternative chunk of code renders a *Buddhabrot* fractal (note: historically *Ganesh* is more accurate). This is a fractal similar to the *Mandelbrot* fractal, and consists of the set of points in the complex plane for which the sequence $z_{n+1} = z_n^2 + c$ does not tend to infinity for $z_0 = 0$ (as described by [Wikipedia](#)). The actual implementation is as mysterious as the previous sentence, on purpose. Luckily, only one part of that code matters: the two lines that read and write data to iteratively update the image.



Memory access

The two code paths have very different memory access patterns. The Buddhabrot access the screen, while the spiral has a more predictable pattern.

The application has been augmented with an interface to - the image buffer is replicated to mem.WriteUInt, which



Meanwhile, P1

```

    // Loop over all line pixels
    for (int i = 0; i < nroSteps; i++) {
        // Perform step (increment / decrement)
        X += XStep; Y += YStep;

        // Get Positions
        uint position_X = Pos(X);
        uint position_Y = Pos(Y);

        // Get Weights and complements
        uint c_weight = Error(X) + Error(Y) >> 8;
        uint weight = c_weight ^ 0xff;

        // Draw pixels
        // Left-Bottom (LB)
        {
            uint clr_b = screen->pixels[position_X + position_Y * SCRWIDTH] & 0xffffffff;
            uint rb = clr_b & 0xff;
            uint gb = clr_b >> 8 & 0xff;
            uint bb = clr_b >> 16 & 0xff;

            uint rr = (( (linecols >> 16) & 255) - rb) * weight >> 8) + rb;
            uint gr = (( (linecols >> 8) & 255) - gb) * weight >> 8) + gb;
            uint br = (( (linecols & 255) - bb) * weight >> 8) + bb;
            uint clr_r = rr + (gr << 8) + (br << 16);
            screen->Plot( position_X, position_Y, clr_r );
        }

        position_X += ~flags & 0b1;
        position_Y += flags & 0b1;
        // Left-Top (LT) or Right-Bottom (RB)
        {
            uint clr_b = screen->pixels[position_X + position_Y * SCRWIDTH] & 0xffffffff;
            uint rb = clr_b & 0xff;
            uint gb = clr_b >> 8 & 0xff;
            uint bb = clr_b >> 16 & 0xff;

            uint rr = (( (linecols >> 16) & 255) - rb) * c_weight >> 8) + rb;
            uint gr = (( (linecols >> 8) & 255) - gb) * c_weight >> 8) + gb;
            uint br = (( (linecols & 255) - bb) * c_weight >> 8) + bb;
            uint clr_r = rr + (gr << 8) + (br << 16);
            screen->Plot( position_X, position_Y, clr_r );
        }
    }
}

```



Today's Agenda:

- Introduction
- Intel: SSE
- Streams
- Vectorization
- Assignment 2



Introduction

Consistent Approach

- (0.) Determine optimization requirements
1. Profile: determine hotspots
2. Analyze hotspots: determine scalability
3. Apply high level optimizations to hotspots
4. Profile again.
5. Parallelize / vectorize / use GPGPU
6. Profile again.
7. Apply low level optimizations to hotspots
8. Repeat steps 7 and 8 until time runs out
9. Report.



Rules of Engagement

1. Avoid Costly Operations
2. Precalculate
3. Pick the Right Data Type
4. Avoid Conditional Branches
5. Early Out
6. Use the Power of Two
7. Do Things Simultaneously



Introduction

S.I.M.D.

Single Instruction Multiple Data:
Applying the same instruction to several input elements.

In other words: if we are going to apply the same sequence of instructions to a large input set, this allows us to do this in parallel (and thus: faster).

SIMD is also known as *instruction level parallelism*.

Examples:

"Give me four random bytes, but they can't be all zero"

```
union { uint a4; unsigned char a[4]; };
do
{
    a[0] = RandomByte();
    a[1] = RandomByte();
    a[2] = RandomByte();
    a[3] = RandomByte();
}
while (a4 == 0);
```



```
unsigned char a[4] = { 1, 2, 3, 4 };
unsigned char b[4] = { 5, 5, 5, 5 };
unsigned char c[4];
*(uint*)c = *(uint*)a + *(uint*)b;
// c is now { 6, 7, 8, 9 }.
```



```

void Game::Tick( float deltaTime )
{
0000000140002C40 movss      dword ptr [rsp+10h],xmm1
0000000140002C46 mov        qword ptr [rsp+8],rcx
0000000140002C48 push       rdi
0000000140002C4C sub        rsp,90h
0000000140002C53 mov        rdi,rs
0000000140002C56 mov        ecx,24h
0000000140002C5B mov        eax,0CCCCCCCCCh
0000000140002C60 rep stos    dword ptr [rdi]
0000000140002C62 mov        rcx,qword ptr [this]

    unsigned char a[4] = { 1, 2, 3, 4 };
0000000140002C6A mov        byte ptr [a],1
0000000140002C6F mov        byte ptr [rsp+35h],2
0000000140002C74 mov        byte ptr [rsp+36h],3
0000000140002C79 mov        byte ptr [rsp+37h],4

    unsigned char b[4] = { 5, 5, 5, 5 };
0000000140002C7E mov        byte ptr [b],5
0000000140002C83 mov        byte ptr [rsp+55h],5
0000000140002C88 mov        byte ptr [rsp+56h],5
0000000140002C8D mov        byte ptr [rsp+57h],5

    unsigned char c[4];
    *(uint*)c = *(uint*)a + *(uint*)b;
0000000140002C92 mov        eax,dword ptr [b]
0000000140002C96 mov        ecx,dword ptr [a]
0000000140002C9A add        ecx,eax
0000000140002C9C mov        eax,ecx
0000000140002C9E mov        dword ptr [c],eax

```

Examples:

"Give me four random bytes, but they can't be all zero"

```

union { uint a4; unsigned char a[4]; };
do
{
    a[0] = RandomByte();
    a[1] = RandomByte();
    a[2] = RandomByte();
    a[3] = RandomByte();
} while (a4 == 0);

```

```

unsigned char a[4] = { 1, 2, 3, 4 };
unsigned char b[4] = { 5, 5, 5, 5 };
unsigned char c[4];
*(uint*)c = *(uint*)a + *(uint*)b;
// c is now { 6, 7, 8, 9 }.

```



Introduction

```

void Game::Tick( float deltaTime )
{
0000000140002250  movss      dword ptr [rsp+10h],xmm1
0000000140002256  mov         qword ptr [rsp+8],rcx
0000000140002258  sub         rsp,38h
    unsigned char a[4] = { 1, 2, 3, 4 };
    unsigned char b[4] = { 5, 5, 5, 5 };
000000014000225F  mov         dword ptr [rsp+40h],5050505h
►| unsigned char c[4];
    *(uint*)c = *(uint*)a + *(uint*)b;
0000000140002267  mov         edx,dword ptr [b]
000000014000226B  mov         dword ptr [rsp+48h],4030201h
0000000140002273  add         edx,dword ptr [a]
0000000140002277  mov         ecx,edx
0000000140002279  mov         eax,edx
;

//radiance = SampleLight( &rand, I, &L, &lightIdx );
//e.x + radiance.y + radiance.z ) > 0) && (dot( N,
//v = true;
//at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
//at t3 factor = diffuse * INVPi;
//at weight = Mis2( directPdf, brdfPdf );
//at cosThetaOut = dot( N, L );
//E * ((weight * cosThetaOut) / directPdf) * (radiance
//random walk - done properly, closely following Smiley
//alive)

;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
E * brdf * (dot( N, R ) / pdf);
alive = true;

```

Examples:

"Give me four random bytes, but they can't be all zero"

```

union { uint a4; unsigned char a[4]; };
do
{
    a[0] = RandomByte();
    a[1] = RandomByte();
    a[2] = RandomByte();
    a[3] = RandomByte();
}
while (a4 == 0);

```

```

unsigned char a[4] = { 1, 2, 3, 4 };
unsigned char b[4] = { 5, 5, 5, 5 };
unsigned char c[4];
*(uint*)c = *(uint*)a + *(uint*)b;
// c is now { 6, 7, 8, 9 }.

```



Introduction

`uint = unsigned char[4]`

Pinging google.com yields: 74.125.136.101
 Each value is an unsigned 8-bit value (0..255).
 Combing them in one 32-bit integer:

$$\begin{aligned} & 101 + \\ & 256 * 136 + \\ & 256 * 256 * 125 + \\ & 256 * 256 * 256 * 74 = 1249740901. \end{aligned}$$

Browse to: <http://1249740901> (works!)

Evil use of this:

We can specify a user name when visiting a website, but any username will be accepted by google. Like this:

<http://infomov@google.com>

Or:

<http://www.ing.nl@1249740901>

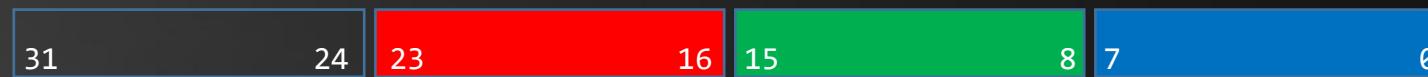
Replace the IP address used here by your own site which contains a copy of the ing.nl site to obtain passwords, and send the link to a ‘friend’.



Introduction

Example: color scaling

Assume we represent colors as 32-bit ARGB values using unsigned ints:



To scale this color by a specified percentage, we use the following code:

```
uint ScaleColor( uint c, float x ) // x = 0..1
{
    uint red = (c >> 16) & 255;
    uint green = (c >> 8) & 255;
    uint blue = c & 255;
    red = red * x, green = green * x, blue = blue * x;
    return (red << 16) + (green << 8) + blue;
}
```



Introduction

31	24	23	16	15	8	7	0
----	----	----	----	----	---	---	---

Example: color scaling

```
    ics
    & (depth < MAXDEPTH)
    c = inside ? 1 : 1.2f;
    nt = nt / nc; ddn = ddn / nc;
    pos2t = 1.0f - nt * ddn;
    D, N );
}
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;

-
refl + refl) && (depth < MAXDEPTH)

D, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lighting
e.x + radiance.y + radiance.z) > 0 && (dot( N
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPi;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Smith
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, R, Pdf
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;
```

```
uint ScaleColor( uint c, float x ) // x = 0..1
{
    uint red = (c >> 16) & 255, green = (c >> 8) & 255, blue = c & 255;
    red = red * x, green = green * x, blue = blue * x;
    return (red << 16) + (green << 8) + blue;
}
```

Improved:

```
MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lighting
e.x + radiance.y + radiance.z) > 0 && (dot( N
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPi;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Smith
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, R, Pdf
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;
```

```
uint ScaleColor( uint c, uint x ) // x = 0..255
{
    uint red = (c >> 16) & 255, green = (c >> 8) & 255, blue = c & 255;
    red = (red * x) >> 8;
    green = (green * x) >> 8;
    blue = (blue * x) >> 8;
    return (red << 16) + (green << 8) + blue;
}
```



Introduction



Example: color scaling

```
uint ScaleColor( uint c, uint x ) // x = 0..255
{
    uint red = (c >> 16) & 255, green = (c >> 8) & 255, blue = c & 255;
    red = (red * x) >> 8, green = (green * x) >> 8, blue = (blue * x) >> 8;
    return (red << 16) + (green << 8) + blue;
}
```

7 shifts, 3 ands, 3 muls, 2 adds

Improved:

```
uint ScaleColor( const uint c, const uint x ) // x = 0..255
{
    uint redblue = c & 0x00FF00FF;
    uint green   = c & 0x0000FF00;
    redblue = ((redblue * x) >> 8) & 0x00FF00FF;
    green = ((green * x) >> 8) & 0x0000FF00;
    return redblue + green;
```

2 shifts, 4 ands, 2 muls, 1 add



Introduction



Example: color scaling

```
uint ScaleColor( uint c, uint x ) // x = 0..255
{
    uint red = (c >> 16) & 255, green = (c >> 8) & 255, blue = c & 255;
    red = (red * x) >> 8, green = (green * x) >> 8, blue = (blue * x) >> 8;
    return (red << 16) + (green << 8) + blue;
}
```

*7 shifts, 3 ands, 3 muls, 2 adds
(15 ops)*

Further improved:

```
uint ScaleColor( const uint c, const uint x ) // x = 0..255
{
    uint redblue = c & 0x00FF00FF;
    uint green   = c & 0x0000FF00;
    redblue = (redblue * x) & 0xFF00FF00;
    green = (green * x) & 0x00FF0000;
    return (redblue + green) >> 8;
}
```

*1 shift, 4 ands, 2 muls, 1 add
(8 ops)*



Introduction

Other Examples

Rapid string comparison:

```
char a[] = "optimization skills rule";
char b[] = "optimization is so nice!";
bool equal = true;
int l = strlen( a );
for ( int i = 0; i < l; i++ )
{
    if (a[i] != b[i])
    {
        equal = false;
        break;
    }
}
```

```
char a[] = "optimization skills rule";
char b[] = "optimization is so nice!";
bool equal = true;
int q = strlen( a ) / 4;
for ( int i = 0; i < q; i++ )
{
    if (((int*)a)[i] != ((int*)b)[i])
    {
        equal = false;
        break;
    }
}
```

Likewise, we can copy byte arrays faster:



```

for (int i = 0; i < q; i++)
00000001400022BD  movsx    rdx, eax
00000001400022C0  test     eax, eax
00000001400022C2  jle      Tmpl8::Game::Tick+87h (01400022D7h)
00000001400022C4  xor     eax, eax
{
    if (((int*)a)[i] != ((int*)b)[i])
00000001400022C6  mov     ecx, dword ptr b[rax*4]
00000001400022CA  cmp     dword ptr [rsp+rax*4], ecx
00000001400022CD  jne      Tmpl8::Game::Tick+87h (01400022D7h)
    for (int i = 0; i < q; i++)
00000001400022CF  inc     rax
00000001400022D2  cmp     rax, rdx
00000001400022D5  jl      Tmpl8::Game::Tick+76h (01400022C6h)
    {
        equal = false;
        break;
    }
}

```

```

char a[] = "optimization skills rule";
char b[] = "optimization is so nice!";
bool equal = true;
int q = strlen( a ) / 4;
for ( int i = 0; i < q; i++ )
{
    if (((int*)a)[i] != ((int*)b)[i])
    {
        equal = false;
        break;
    }
}

```



Introduction

SIMD using 32-bit values - Limitations

Mapping four chars to an int value has a number of limitations:

$$\{100, 100, 100, 100\} + \{1, 1, 1, 200\} = \{101, 101, 102, 44\}$$

$$\{ 100, 100, 100, 100 \}^* \{ 2, 2, 2, 2 \} = \{ \dots \}$$

$$\{100, 100, 100, 200\}^* 2 = \{200, 200, 201, 144\}$$

In general:



Introduction

SIMD using 32-bit values - Limitations

Ideally, we would like to see:

- Isolated streams
- Support for more data types (char, short, uint, int, float, double)
- An easy to use approach

Meet SSE!

```
rics
  & (depth < MAXDEPTH)
  n = inside ? 1 : 1.0f;
  nt = nt / nc, ddn = ddc;
  os2t = 1.0f - nnt * nnt;
  D, N );
}

at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;

-
refl + refl)) && (depth < MAXDEPTH)
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lightDir,
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e.y + radiance.z ) > 0);
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e.y + radiance.z ) > 0);
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e.y + radiance.z ) > 0);

v = true;
at brdfPpdf = EvaluateDiffuse( L, N ) * Psurvive;
at dot3 factor = diffuse * INVPi;
at weight = Mis2( directPpdf, brdfPpdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPpdf) * (radiance
random walk - done properly, closely following Smiley
ive);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;
```



Today's Agenda:

- Introduction
- Intel: SSE
- Streams
- Vectorization
- Assignment 2



SSE

A Brief History of SIMD

Early use of SIMD was in vector supercomputers such as the CDC Star-100 and TI ASC (image).

Intel's MMX extension to the x86 instruction set (1996) was the first use of SIMD in commodity hardware, followed by Motorola's AltiVec (1998), and Intel's SSE (P3, 1999).

SSE:

- 70 assembler instructions
- Operates on 128-bit registers
- Operates on vectors of 4 floats.



SSE

SIMD Basics

C++ supports a 128-bit vector data type: `_m128`

Henceforth, we will pronounce to this as 'quadfloat'. ☺

`_m128` literally is a small array of floats:

```
union { __m128 a4; float a[4]; };
```

Alternatively, you can use the integer variety `_m128i`:

```
union { __m128i a4; int a[4]; };
```



SSE

SIMD Basics

We operate on SSE data using *intrinsics*: in the case of SSE, these are keywords that translate to a single assembler instruction.

Examples:

```
__m128 a4 = _mm_set_ps( 1, 0, 3.141592f, 9.5f );
__m128 b4 = _mm_setzero_ps();
__m128 c4 = _mm_add_ps( a4, b4 ); // not: __m128 = a4 + b4;
__m128 d4 = _mm_sub_ps( b4, a4 );
```

Here, ‘_ps’ stands for *packed scalar*.



SSE

SIMD Basics

Other instructions:

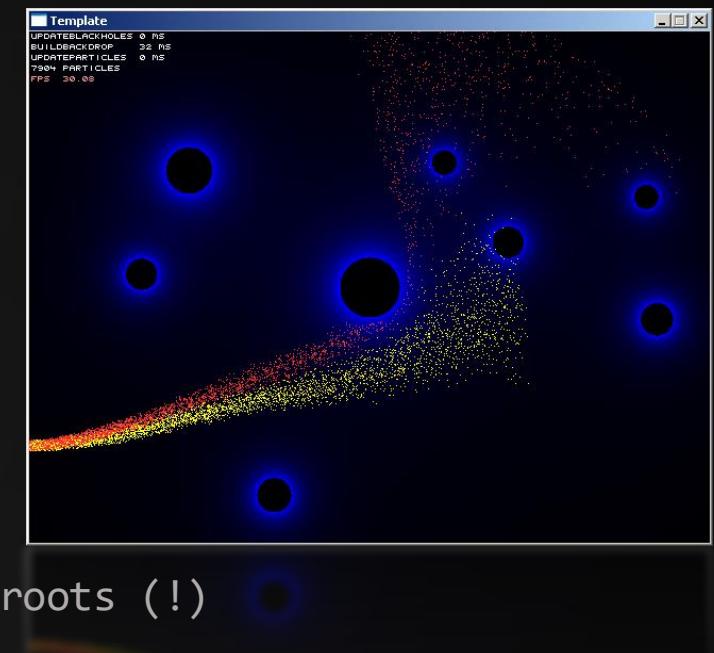
```
_m128 c4 = _mm_div_ps( a4, b4 ); // component-wise division
_m128 d4 = _mm_sqrt_ps( a4 );    // four square roots
_m128 d4 = _mm_rcp_ps( a4 );    // four reciprocals
_m128 d4 = _mm_rsqrt_ps( a4 );   // four reciprocal square roots (!)

_m128 d4 = _mm_max_ps( a4, b4 );
_m128 d4 = _mm_min_ps( a4, b4 );
```

Keep the assembler-like syntax in mind:

```
_m128 d4 = dx4 * dx4 + dy4 * dy4;

_m128 d4 = _mm_add_ps(
    _mm_mul_ps( dx4, dx4 ),
    _mm_mul_ps( dy4, dy4 )
);
```



CODING TIME



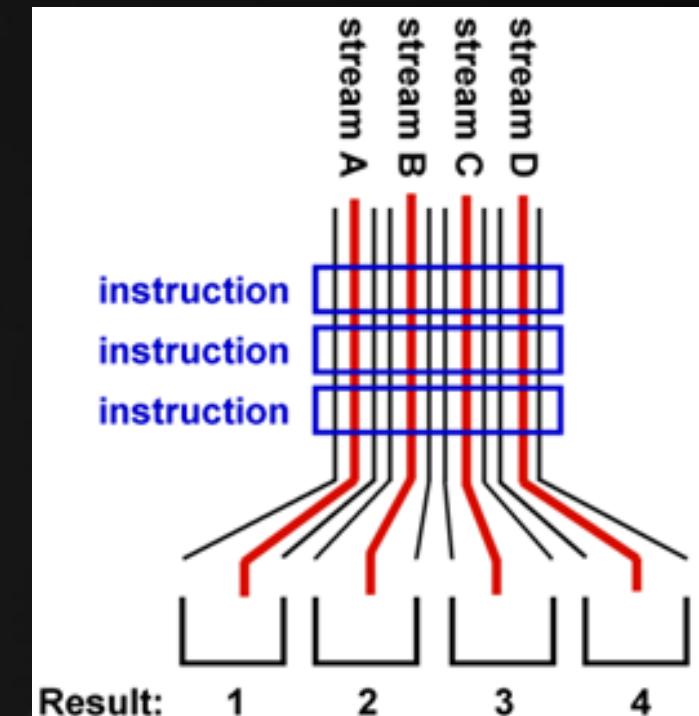
SSE

SIMD Basics

In short:

- Four times the work at the price of a single scalar operation (if you can feed the data fast enough)
- Potentially even better performance for min, max, sqrt, rsqrt
- Requires four independent streams.

And, with AVX we get _m256...



```

rics
  & (depth < MAXDEPTH)
  n = inside ? 1 : 1.0f;
  nt = nt / nc; ddn = ddc;
  pos2t = 1.0f - nt * nnt;
  R = (D * nnt - N * (ddn
  E * diffuse;
  = true;

  refl + refr)) && (depth < MAXDEPTH);
  N );
  refl * E * diffuse;
  = true;

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &light,
e.x + radiance.y + radiance.z ) > 0) && (dot( N,
  v = true;
  brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
  at3 factor = diffuse * INVPi;
  at weight = Mis2( directPdf, brdfPdf );
  at cosThetaOut = dot( N, L );
  E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Smiley
ive);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
survive;
pdf;
  n = E * brdf * (dot( N, R ) / pdf);
  = true;

```



Today's Agenda:

- Introduction
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Streams

SIMD According To Visual Studio

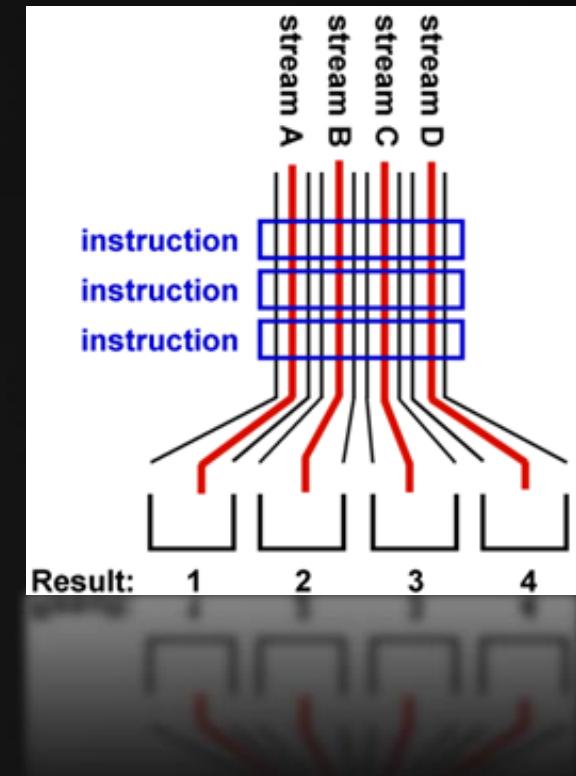
```

vec3 A( 1, 0, 0 );
vec3 B( 0, 1, 0 );
vec3 C = (A + B) * 0.1f;
vec3 D = normalize( C );

```

The compiler will notice that we are operating on 3-component vectors, and it will use SSE instructions to speed up the code. This results in a modest speedup. Note that one lane is never used at all.

To get maximum throughput, we want four independent streams, running in parallel.



Streams

SIMD According To Visual Studio

```
vec3 A( 1, 0, 0 );
vec3 B( 0, 1, 0 );
vec3 C = (A + B) * 0.1f;
vec3 D = normalize( C );
```

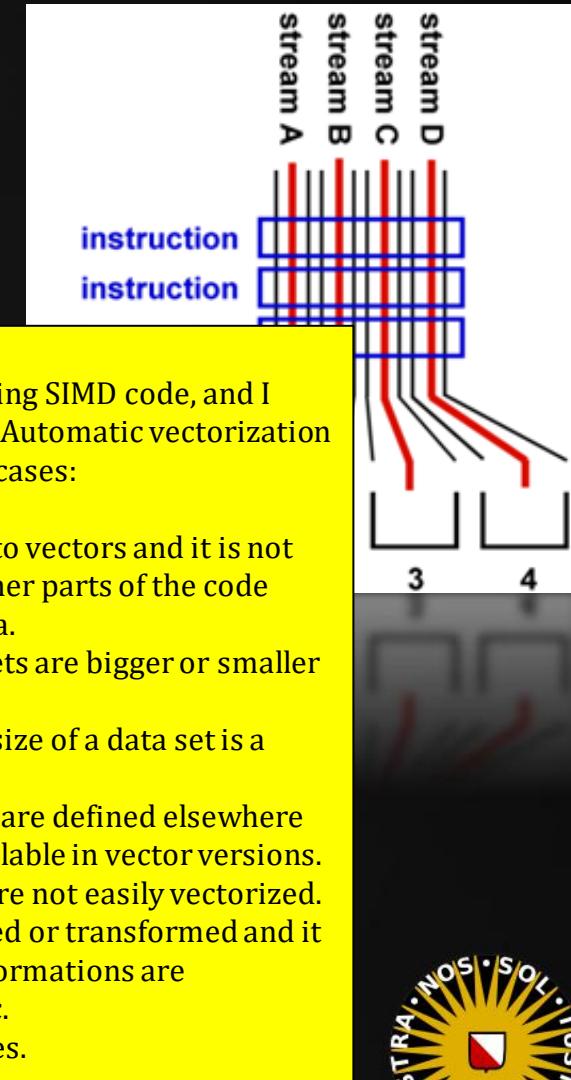
The compiler will notice that we are operating on vectors, and it will use SSE instructions. This results in a modest speedup. Note that

To get maximum throughput, we want running in parallel.

Agner Fog:

"Automatic vectorization is the easiest way of generating SIMD code, and I would recommend to use this method when it works. Automatic vectorization may fail or produce suboptimal code in the following cases:

- when the algorithm is too complex.
- when data have to be re-arranged in order to fit into vectors and it is not obvious to the compiler how to do this or when other parts of the code needs to be changed to handle the re-arranged data.
- when it is not known to the compiler which data sets are bigger or smaller than the vector size.
- when it is not known to the compiler whether the size of a data set is a multiple of the vector size or not.
- when the algorithm involves calls to functions that are defined elsewhere or cannot be inlined and which are not readily available in vector versions.
- when the algorithm involves many branches that are not easily vectorized.
- when floating point operations have to be reordered or transformed and it is not known to the compiler whether these transformations are permissible with respect to precision, overflow, etc.
- when functions are implemented with lookup tables.



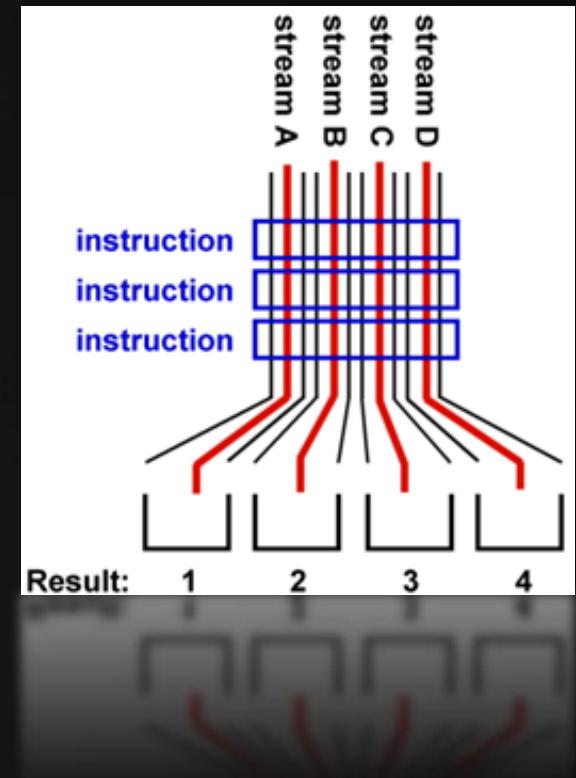
Streams

SIMD According To Visual Studio

```

float Ax = 1, Ay = 0, Az = 0;
float Bx = 0, By = 1, Bz = 0;
float Cx = (Ax + Bx) * 0.1f;
float Cy = (Ay + By) * 0.1f;
float Cz = (Az + Bz) * 0.1f;
float l = sqrtf( Cx * Cx + Cy * Cy + Cz * Cz);
float Dx = Cx / l;
float Dy = Cy / l;
float Dz = Cz / l;

```



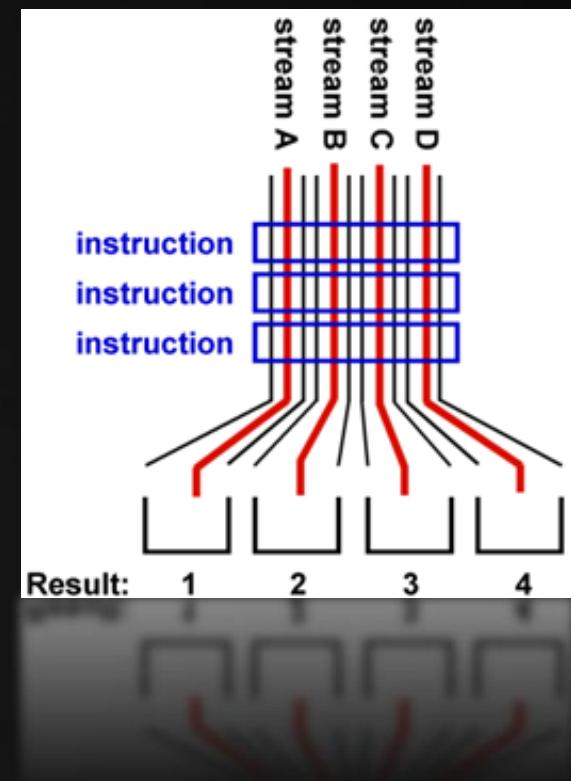
"Scalar decomposition"



Streams

SIMD According To Visual Studio

```
float Ax[4] = {...}, Ay[4] = {...}, Az[4] = {...};  
float Bx[4] = {...}, By[4] = {...}, Bz[4] = {...};  
float Cx[4] = ...;  
float Cy[4] = ...;  
float Cz[4] = ...;  
float l[4] = ...;  
float Dx[4] = ...;  
float Dy[4] = ...;  
float Dz[4] = ...;
```



Streams

SIMD According To Visual Studio

```

rics
& (depth < MAXDEPTH)
nt = inside ? 1 : 1.0f;
nt = nt / nc; ddn = ddn / nc;
pos2t = 1.0f - nt * nnt;
D, N );
)
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;

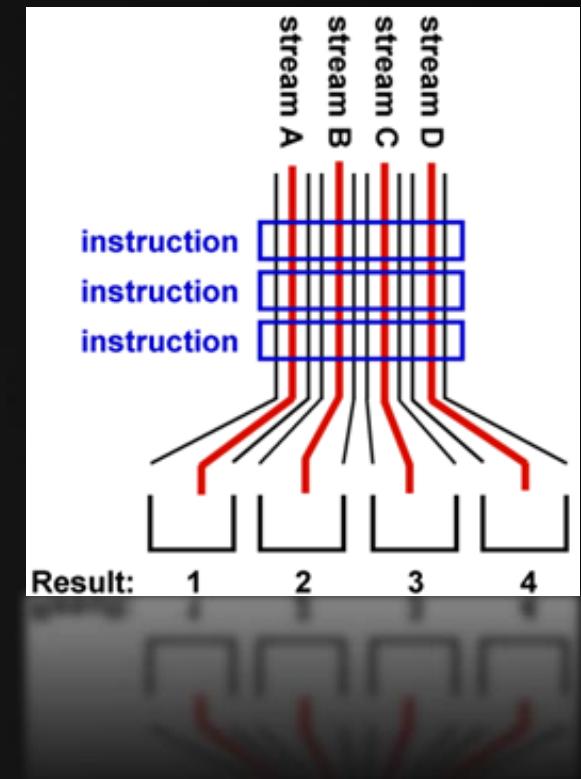
-
refl + refl)) && (depth < MAXDEPTH);
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lightDir,
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * (weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Smiley
alive);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;

```



Streams

SIMD According To Visual Studio

```

rics
& (depth < MAXDEPTH)
nt = inside ? 1 : 1.0f;
nt = nt / nc; ddn = ddn * nc;
pos2t = 1.0f - nt * nnt;
D, N );
)
at a = nt - nc, b = nt + nc;
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;

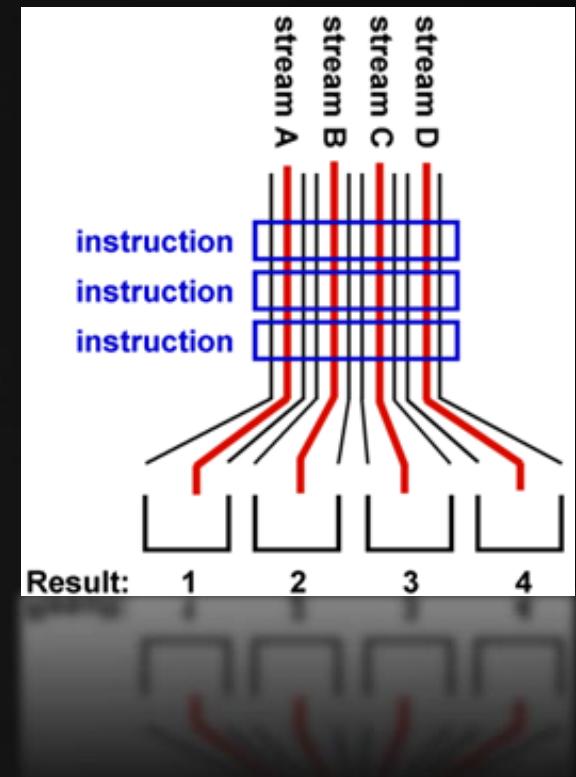
-
refl + refl)) && (depth < MAXDEPTH);
D, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse,
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lightDir,
e.x + radiance.y + radiance.z) > 0) && (dot( N,
e, L ) > 0);
v = true;
at brdfPpdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPpdf, brdfPpdf );
at cosThetaOut = dot( N, L );
E * (weight * cosThetaOut) / directPpdf) * (radiance
random walk - done properly, closely following Smiley
alive);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf,
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
ision = true;

```



Streams

SIMD According To Visual Studio

```

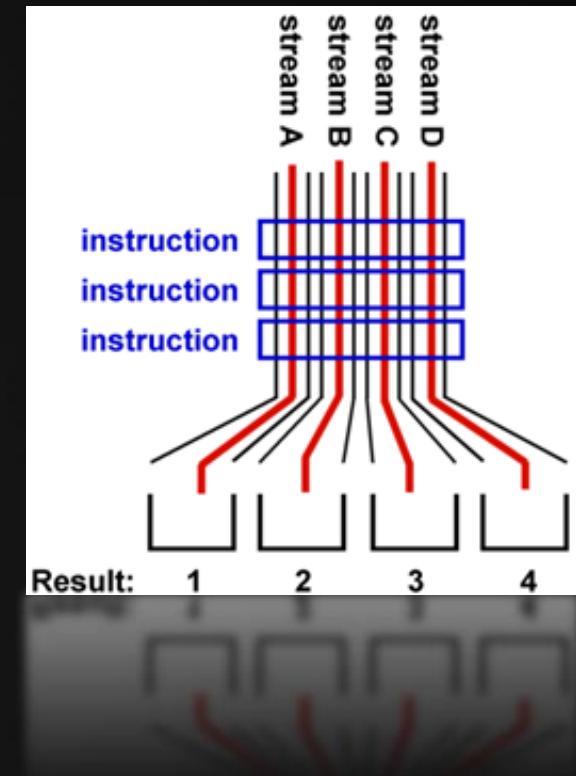
__m128 Ax4 = _mm_set_ps( Ax[0], Ax[1], Ax[2], Ax[3] );
__m128 Ay4 = _mm_set_ps( Ay[0], Ay[1], Ay[2], Ay[3] );
__m128 Az4 = _mm_set_ps( Az[0], Az[1], Az[2], Az[3] );
__m128 Bx4 = { ... }, By4 = { ... }, Bz4 = { ... };
__m128 X4 = _mm_set1_ps( 0.1f );
__m128 Cx4 = _mm_mul_ps( _mm_add_ps( Ax4, Bx4 ), X4 );
__m128 Cy4 = _mm_mul_ps( _mm_add_ps( Ay4, By4 ), X4 );
__m128 Cz4 = _mm_mul_ps( _mm_add_ps( Az4, Bz4 ), X4 );
__m128 I4 = ...;
__m128 Dx4 = ...;
__m128 Dy4 = ...;
__m128 Dz4 = ...;

v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPi;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * (weight * cosThetaOut) / directPdf * (radiance.x + radiance.y + radiance.z) > 0 && (dot( N, L ) > 0);
if( v )
    cout << "Random walk - done properly, closely following Smith's  

        random walk algorithm." << endl;
else
    cout << "Random walk - done properly, closely following Smith's  

        random walk algorithm." << endl;
}

```



Streams

SIMD Friendly Data Layout

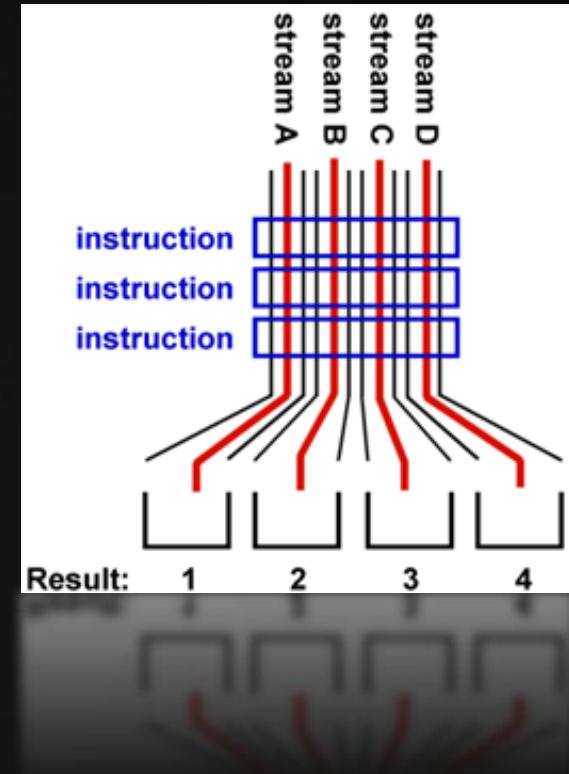
Consider the following data structure:

```
struct Particle
{
    float x, y, z;
    int mass;
};

Particle particle[512];
```

AoS

SoA



Streams

SIMD Data Naming Conventions

```
rics  
    & (depth < MAXDEPTH)  
    union { float x[512]; __m128 x4[128]; };  
    union { float y[512]; __m128 y4[128]; };  
    union { float z[512]; __m128 z4[128]; };  
    union { int mass[512]; __m128i mass4[128]; };
```

Notice that SoA is breaking our OO...

Consider adding the struct name to the variables:

```
float particle_x[512];
```

Or put an amount of particles in a struct.

Also note the convention of adding ‘4’ to any SSE variable.



Today's Agenda:

- Introduction
- Intel: SSE
- Streams
- Vectorization
- Assignment 2



P2

```

rics
    & (depth < MAXDEPTH)
    = inside ? 1 : 1.0f;
    nt = nt / nc; ddn = ddn / nc;
    os2t = 1.0f - nnt * nnt;
    D, N );
}
}

at a = nt - nc, b = nt + nc, i
at Tr = 1 - (R0 + (1 - R0) *
Tr) R = (D * nnt - N * (ddn
E * diffuse;
= true;

-
refl + refr)) && (depth < MAXDEPTH);

D, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely
if;
radiance = SampleLight( &rand, I, &L, &lightDir,
e.x + radiance.y + radiance.z) > 0) && (dot( N,
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radiance
random walk - done properly, closely following Smiley
ive)

;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
survive;
pdf;
E * brdf * (dot( N, R ) / pdf);
= true;

```



Assignment P2 – Cache Simulator

Final assignment description P2 - INFOMOV
Jeroen Bokhorst, 2024

This document describes the requirements for the second assignment for the INFOMOV course. For this assignment, you will extend a simple cache simulator, which currently implements a fully associative cache.

The base code in game.cpp renders a spiral. The contents of a simulated low-level memory system (L1 cache) are fully visualized in real-time. Eight colors are used; darker ones mean less recently used. The assignment requires the cache to use a random eviction policy, no place of the spiral is currently known.

An efficient chunk of code renders a Buddhabrot fractal (more accurate, faster). The cache is fully implemented, and contains a set of points in the complex plane. The algorithm is an iterative random walk, and iterates until it reaches a point within a radius of 2²⁴. It does not have to iterate for a set of points in the complex plane. An efficient implementation is an improvement on the first sentence, or worse, lucky, only one set of that code matters: the two free fall read and write data to memory under the image.

Memory access

The two code paths have very different memory access patterns. The Buddhabrot rendering has a more predictable pattern, while the spiral has a more unpredictable pattern. The assignment has been augmented with an pseudo-random number generator to improve the predictability of the spiral's memory access pattern.

Implementation

The assignment is split into three parts:

- Part 1: Implement the cache simulator. This part is worth 10% of the grade.
- Part 2: Implement the Buddhabrot rendering. This part is worth 10% of the grade.
- Part 3: Implement the spiral rendering. This part is worth 10% of the grade.

/INFOMOV/

END of “SIMD (1)”

next lecture: “Caching (2)”

